

# Detecting categorical perception in continuous discrimination data

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FOR LANGUAGE AND  
COMMUNICATION



# Categorical perception

## identification

- same category = same label

## discrimination

- same category = difficult discrimination

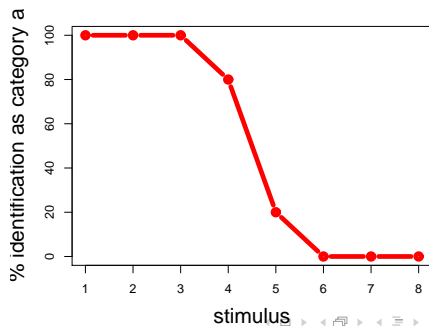
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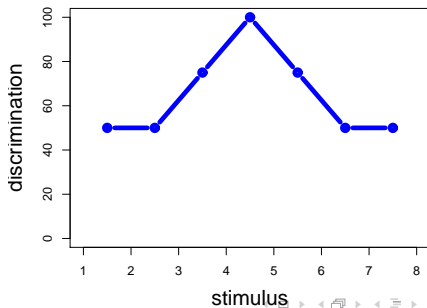
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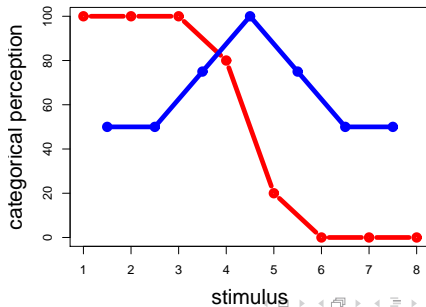
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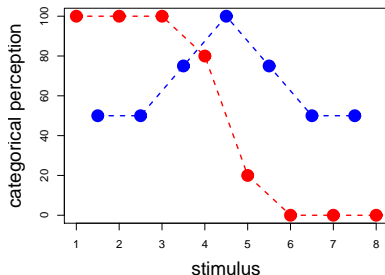
## discrimination

- same category = difficult discrimination



# A problem with previous studies

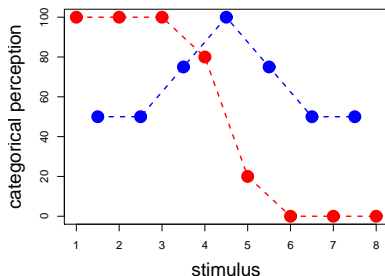
- small number of different stimuli
- repeated multiple times



Rogers & Davis (2009): such design increases listeners' categorical bias

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# The solution, and a remaining problem

- Rogers & Davis' (2009) solution:  
**test categorical perception 'continuously'**,  
i.e. on a densely-sampled phonetic continuum, without repetition
- remaining problem with Rogers & Davis:  
(indentification results: logistic regression,)  
**discrimination results: non-continuous method of analysis**

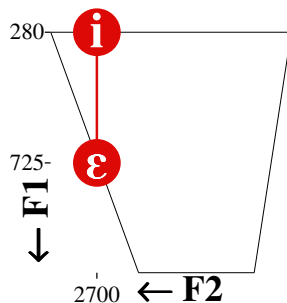


# The aim of the present study

to provide a **continuous analysis method**  
for continuous discrimination data

# Part of a larger experiment<sup>1</sup>

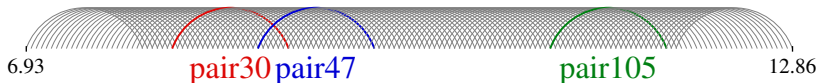
- vowel continuum between /i/ and /ε/
- discrimination along the F1 dimension



<sup>1</sup>Chládková & Benders (in prep.).

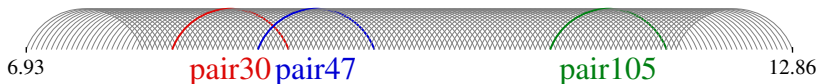
# Stimuli

- **260 different vowels = 130 stimulus pairs**
- equal steps between 280 Hz and 725 Hz (6.93 erb and 12.86 erb)

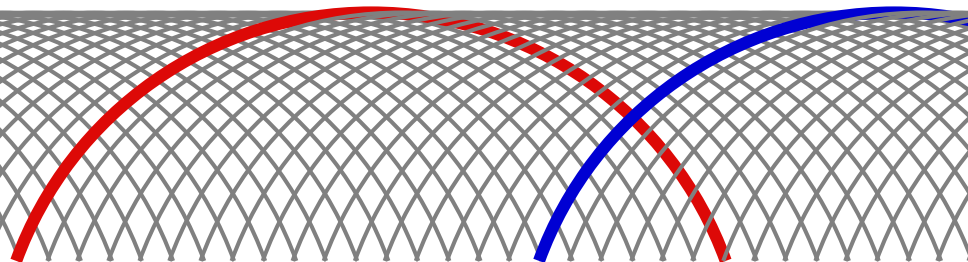


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# Stimuli



pair30 pair4

# Testing procedure

- AX task
- each of the 130 stimulus pairs included twice, i.e.  $a - b$  in one trial,  $b - a$  in the other trial
- the auditory F1 distance is always the same
- **Participants:** 62 monolingual Czechs
- **Question:** How many categories do they have along the continuum?

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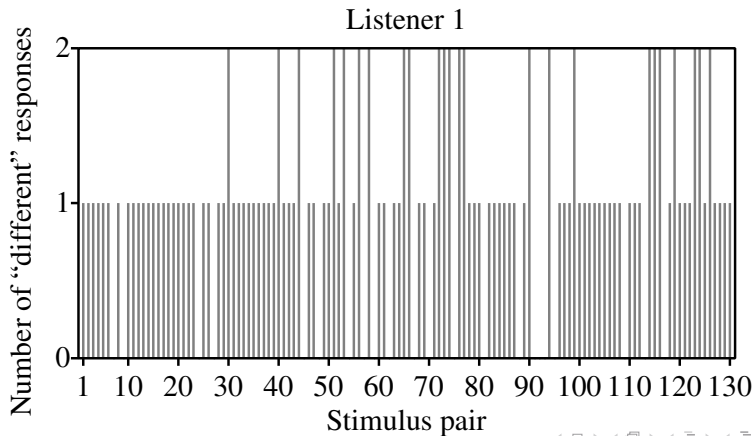


# Data: visual inspection

# Visual inspection

Raw data: max 2 'different' responses / pair: peaks hard to find

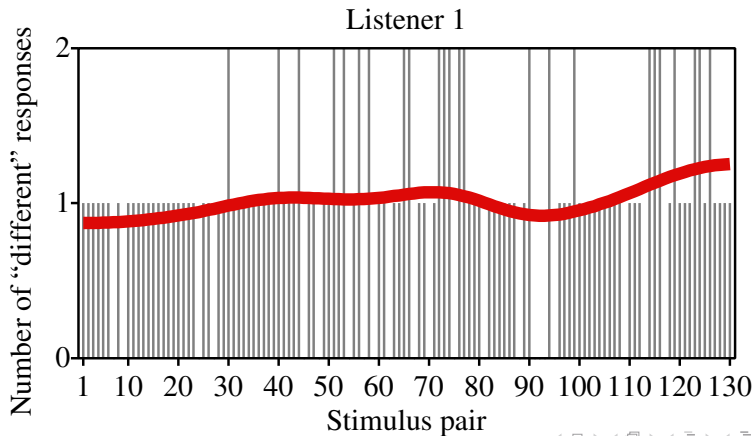
Smoothed data (convolution with a Gaussian): inspection possible



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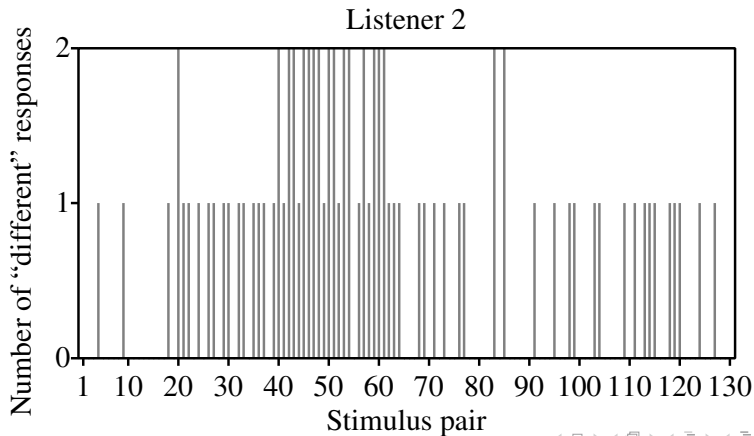
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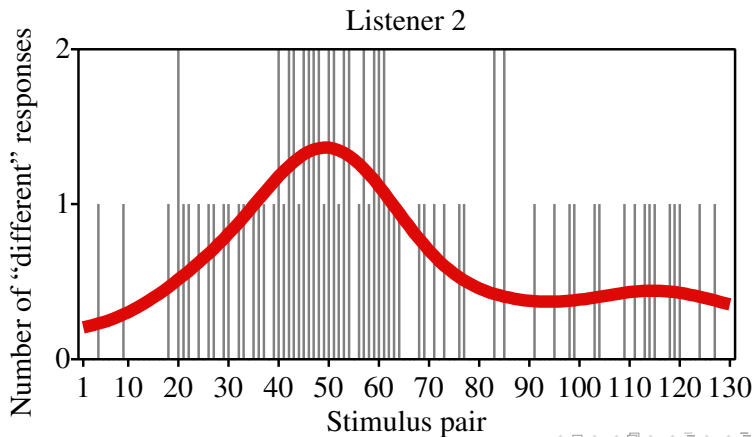
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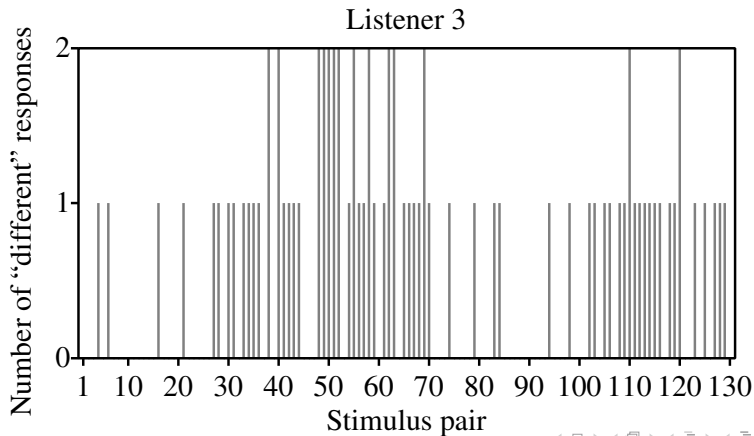
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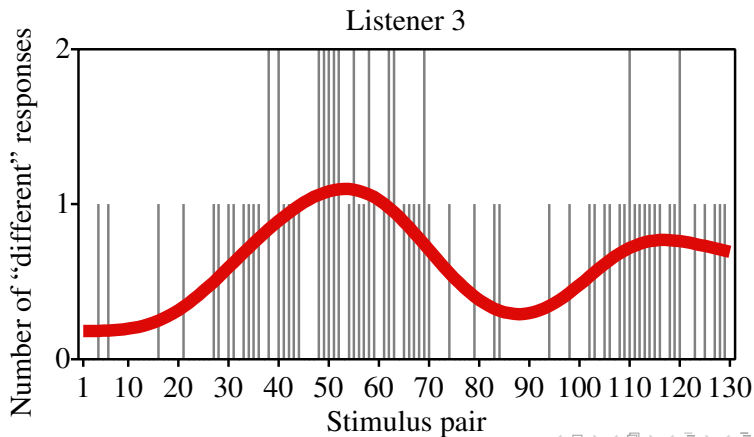
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# Data: analysis



# Analysis: estimate the ‘best’ number of peaks

- per listener, **model** the data with **every possible number of discrimination peaks**
- estimate the **best value of the parameters** that define a model with  $n$  discrimination peaks
  - 0 peaks:  $p_{const}$
  - 1 peak:  $p_{min}, p_{max}, \mu, \sigma$
  - 2 peaks:  $p_{min}, p_{1max}, \mu_1, \sigma_1, p_{2max}, \mu_2, \sigma_2$
  - ...
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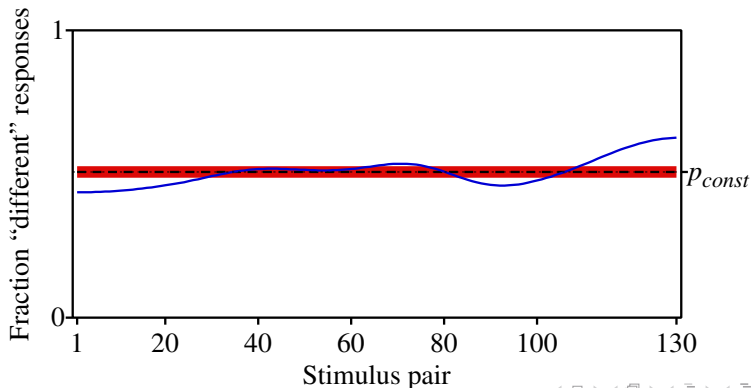
# Model: listener 1

Best fit = 0 peaks

⇒ listens acoustically or has one category

(no evidence for more,  $p = 0.11$ )

— Smoothed data  
- - - Model  
— Smoothed model

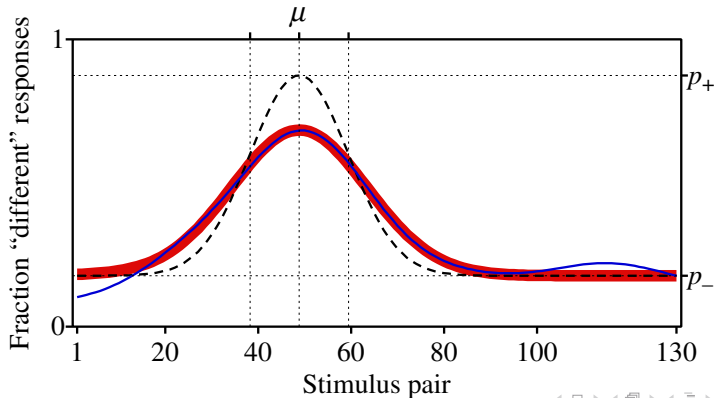


# Model: listener 2

Best fit = 1 peak

⇒ has at least two categories,  $p = 2.1 \cdot 10^{-12}$   
(no evidence for more,  $p = 0.28$ )

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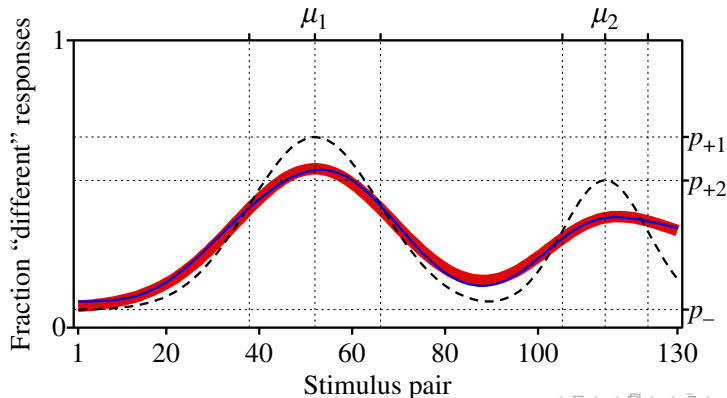
# Model: listener 3

Best fit = 2 peaks

⇒ has at least three categories,  $p = 0.00011$

(no evidence for more,  $p = 0.93$ )

— Smoothed data  
- - - Model  
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# Conclusions

## Method of analysis of continuous discrimination data

- finds the plausible (minimum) number of categories
- estimates location and crispness of category boundaries
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Thank you.

# Maximum-likelihood fit: algorithm

→ the algorithm for 2 peaks

parameters:  $p_{min}$ ,  $p_{1max}$ ,  $\mu_1$ ,  $\sigma_1$ ,  $p_{2max}$ ,  $\mu_2$ ,  $\sigma_2$

- 1 assign random values to the 7 parameters
- 2 randomly change the 7 parameters a little bit
- 3 check whether  $LL$  improves (becomes less negative)
- 4 if  $LL$  improves, keep the values of the parameters
- 5 repeat steps 2 - 4 1000 times
- 6 repeat steps 1 - 5 100 times
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